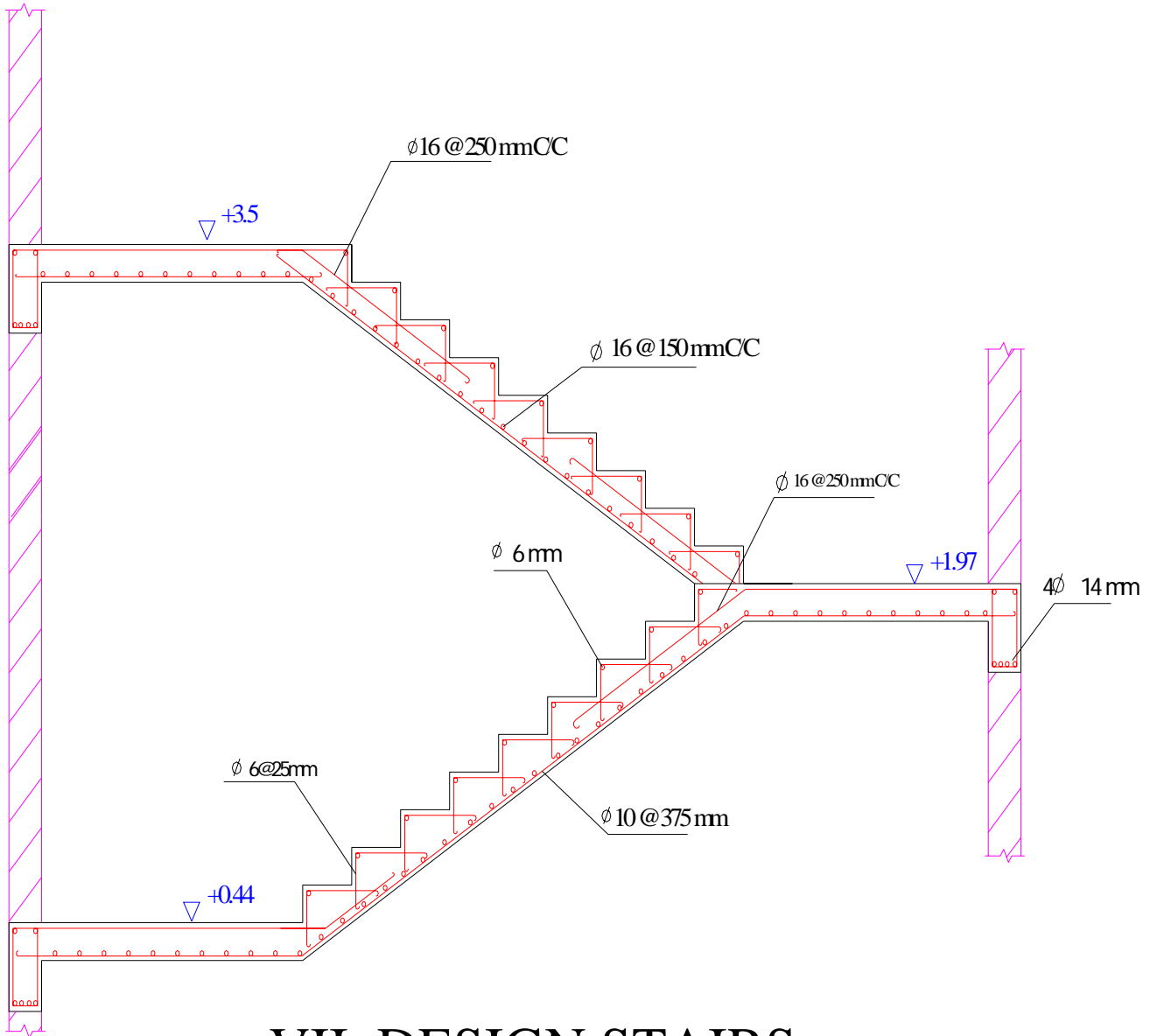


King Faisal University
College of Architecture and Planning
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Building Structure I
Reinforce Concrete Design
0525 – 351

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VII. DESIGN STAIRS

CHAPTER VII

Design Of Reinforced Concrete Stairs

Stairs are constructed to provide access to the different floor levels, within buildings. They consist of a number of steps arranged in series.

Most of stairs are designed as supported one-way slabs

7.1. DEFINITIONS

The definitions of some technical terms which are used in connection with the planning and design of stairs are shown in Figure (7.1).

1. Going (G): The horizontal distance of the upper surface of a step.
2. Rise (R): The vertical distance between horizontal of two consecutive steps.
3. Waist (h) : The least thickness of the stairs slab.
4. Landing : The horizontal platform which is usually provided at the beginning and the end of series of steps.
5. Flight : Comprised of a number of steps provided between two consecutive landing.

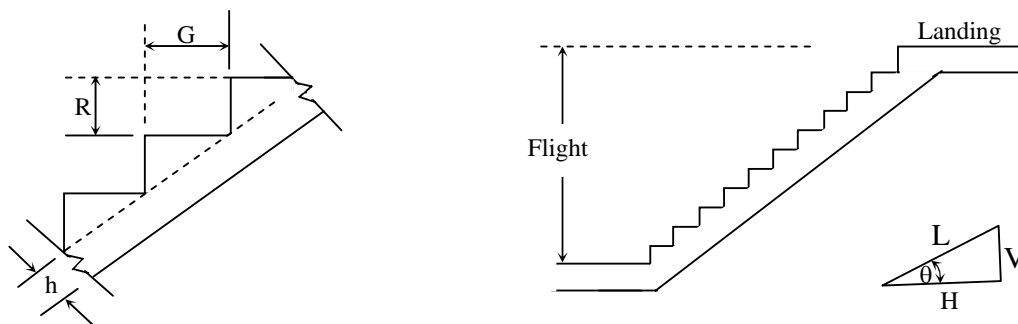


Figure (7.1) Particulars of stairs

7.2. GENERAL REQUIREMENTS:

1. There should be an equal number of steps between consecutive floors, and steps should have identical rises and goings.
2. Rise should not be greater than 17 cm, and the going not less than 22.5 cm

$$R \leq 17 \text{ cm}$$

$$G \geq 22.5 \text{ cm}$$
3. The slope to exterior from 0.2 to 0.3 for reduce the horizontal surface of stairs

7.3. TYPE OF STAIRS:

For the purpose of analysis and design, stairs may classify in two groups:

1) Stairs Spanning Transversely, characterize be:

- a) Stairs simply supported at each side by a wall or beam.
- b) Stairs cantilevering from a wall or beam at one side only.
- c) Stairs cantilevering across a central sloping beam.

2) Stairs Spanning Longitudinally,

Supported at the top and bottom of the flight and are unsupported along the sides.

Referring to Figure (7.2), which shows four common supporting systems of a typical staircase involving two flights, the supporting elements may be:

1) Beams provided at the top and bottom of the actual stairs,

As shown in Fig.(7.2.a), Naturally these beams must be supported in some manner.

2) Beams or walls provided at both outside edges of the landings,

As shown in Fig.(7.2.b), A beam is usually available at the edge of the floor landing, but a special beam or wall has to be provided at the edge of the intermediate landing,

3) Landing slabs which span transversely and are supported by beams or walls at their outsider edges,

As shown in Fig.(7.2.c), Normally, beams are available at the two edges of the floor landing, but special provision have to be mad support intermediate landings at their edges.

4) A combination of a beam, or a wall, at one edge and transversely supported slab the other edge

As shown in Fig.(7.2.d)

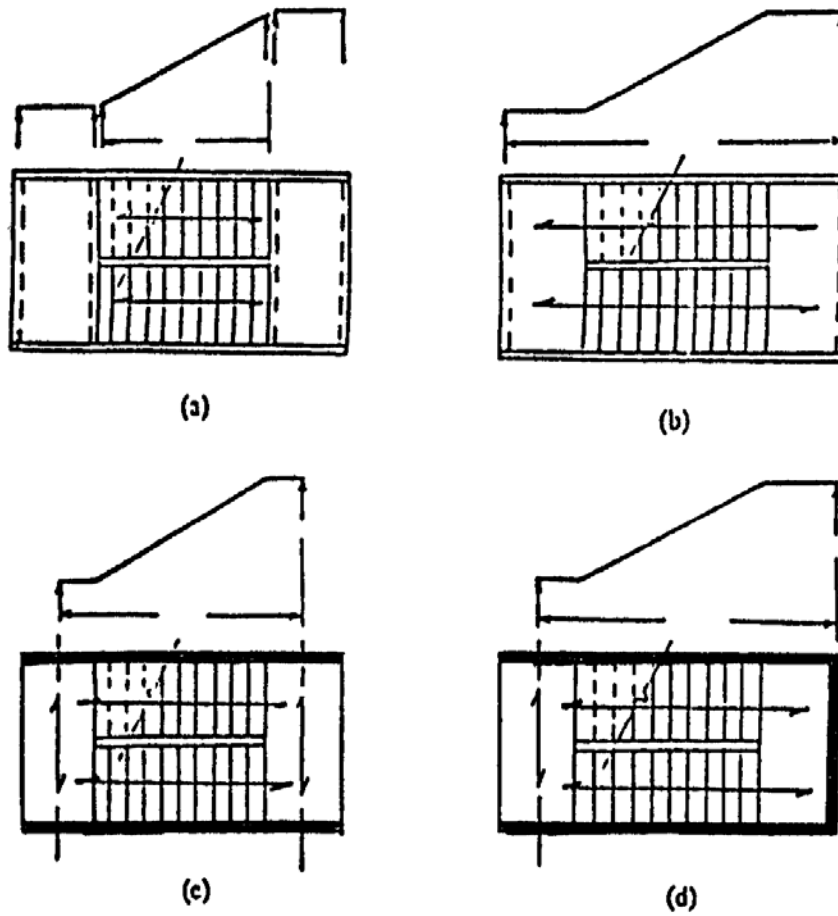


Figure (7.2); Common supporting systems of longitudinally supported stairs

7.4. PRINCIPAL STAIRS

Figure (7.3) and Figure (7.4) show a typical staircase of an Office building. The story height is 3.00 m and a typical step has a rise $R=15$ cm, and a going $G=30$ cm. Design the stairs for the following data:

- Live load = 5 kN/m^2
- $f'_c = 25 \text{ MPa}$, $f_y = 400 \text{ MPa}$ $cc = 20 \text{ mm}$

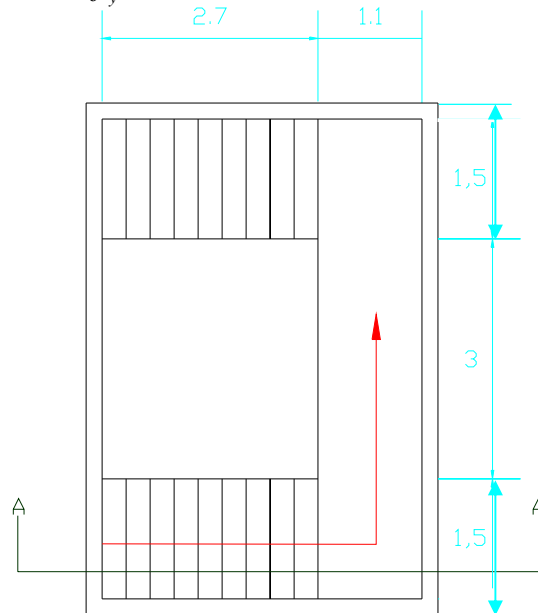


Figure (7.3): Horizontal Stair Dimensions

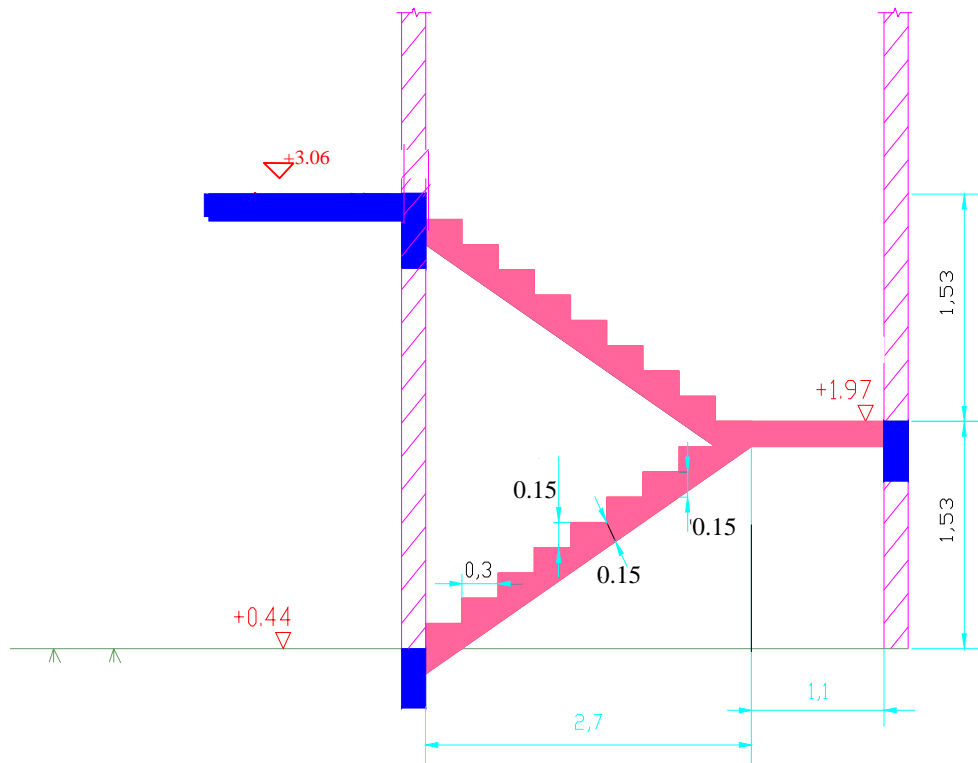


Figure (7.4): Heights of Stair

I. DIMENSIONS:

I.1. Slope Angle of the Stair Slab:

$$\theta = \tan^{-1} \frac{V}{H} = \tan^{-1} \frac{1.53}{2.70} = 29.54^\circ \quad O.K$$

I.2. Length of Stair:

$$L = \sqrt{(1.53)^2 + (2.7)^2} = 3.1m = 3100mm$$

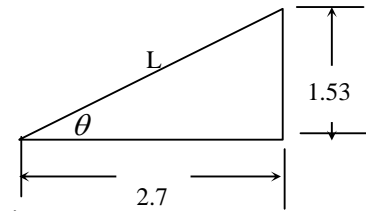
I.3. Thickness of Stair :

For control the deflection (h) .Using ACI Code Deflection Conditions

$$h_{\min} = \frac{L}{24} \quad (\text{one end continuous slab})$$

$$h_{\min} = \frac{3100}{24} = 129.2mm \approx 130mm$$

Use $h = 150mm = 15 \text{ cm}$



II. LOAD CALCULATIONS:

II.1. Load on the Stair Landing:

$$\text{Weight of landing:} \quad = 0.15 \times 1 \times 1 \times 24 = 3.6kN/m^2$$

Finishing:

$$\text{Tiles} \quad = 0.44 kN/m^2$$

$$\text{Cement mortar} \quad = 0.4 kN/m^2$$

$$\text{Plaster} \quad = 0.4 kN/m^2$$

$$\text{Additional load:} \quad = 0.46 kN/m^2$$

$$\sum DL = 5.30kN/m^2$$

$$\sum L.L = 5 kN/m^2$$

Design load:

$$U = (1.2 \times DL) + (1.6 \times LL)$$

$$U_1 = (1.2 \times 5.30) + (1.6 \times 5) = 14.306 kN/m^2$$

II.2. Load on Stair Slab:

$$\text{Weight of slab:} \quad = 0.15 \times 1 \times 1 \times 24 = 3.6 kN/m^2$$

Weight of steps:

$$= \frac{1}{2} \times 0.3 \times 0.15 \times 24 = 0.54kN/m^2$$

Finishing:

$$\text{Tiles} \quad = 0.44 kN/m^2$$

$$\text{Cement mortar:} \quad = 0.4 kN/m^2$$

Plaster = 0.4 kN/m^2
 Additional load = 0.5 kN/m^2
 Total load

$$\sum DL = 5.88 \text{ kN/m}^2$$

$$\sum L.L = 5 \text{ kN/m}^2$$

Design load:

$$U = (1.2 \times DL) + (1.6 \times LL)$$

$$U_2 = (1.2 \times 5.88) + (1.6 \times 5) = 15.56 \text{ kN/m}^2$$

III. STRUCTURAL ANALYSIS

III.1. Reactions:

$$\sum M_A = 0 = (15.56 \times 2.7) \times 1.35 + (14.36 \times 1.1) \times 3.25 - 3.8R_B$$

$$0 = 56.716 + 51.337 - 3.8R_B$$

$$R_B = \frac{108.05}{3.8} = 28.44 \text{ kN}$$

$$\sum Y = 0 = 15.56 \times 2.7 + 14.36 \times 1.1 \times -28.44 - R_A$$

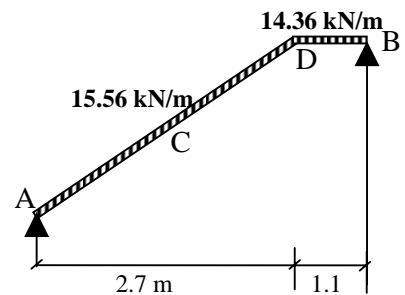
$$R_A = 57.808 - 28.44 = 29.37 \text{ kN}$$

III.2. Moments:

- The positive moment at C

$$M_c = -(15.56 \times 1.35) \times 0.675 + 29.37 \times 1.35$$

$$= -14.179 + 39.65 = 25.47 \text{ kN.m}$$



III.3. Diagrams:

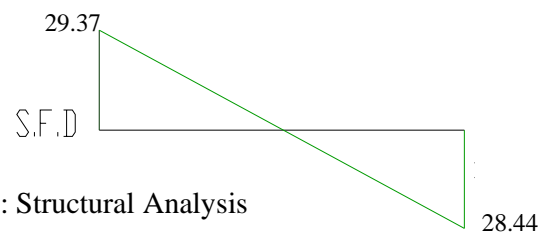
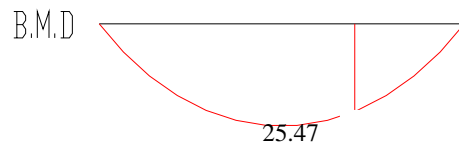
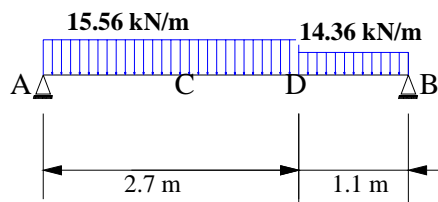


Figure (7.5): Structural Analysis

IV. CALCULATION OF STEEL REINFORCEMENT:**IV.1. Positive Moment (Main Reinforcement):**

Use $\phi_b = 14 \text{ mm}$, Concrete Cover = 20mm , $M_u = 25.47 \text{ kN.m}$,

$$M_n = \frac{M_u}{\phi} = \frac{25.47}{0.9} = 28.3 \text{ kN.m} \quad f'_c = 25 \text{ MPa} \quad f_y = 400 \text{ MPa}$$

Effective depth:

$$d = h - \frac{\phi_b}{2} - cc$$

$$d = 150 - \frac{14}{2} - 20 = 123 \text{ mm}$$

Area of steel:

$$m = \frac{f_y}{0.85 f'_c} = \frac{400}{0.85 \times 25} = 18.81$$

$$R_n = \frac{M_n}{bd^2} = \frac{28.3}{1000 \times (0.124)^2} = 1.841$$

$$\rho = \frac{1}{m} \left[1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right]$$

$$\rho = \frac{1}{18.81} \left[1 - \sqrt{1 - \frac{2 \times 18.81 \times 1.841}{400}} \right]$$

$$\rho = 0.0048$$

Check ρ

$$\rho_{\min} = \frac{1.4}{f_y} = 0.0035$$

$$\rho_{\max} = 0.75 \left[0.85 \times 0.85 \times \frac{25}{400} \times \left(\frac{600}{600 + 400} \right) \right] = 0.02$$

$$\rho_{\min} = 0.0035 < \rho = 0.0048 < \rho_{\max} = 0.02$$

$$A_s = \rho \cdot b \cdot d = 0.0048 \times 1000 \times 124 = 595.2 \text{ mm}^2$$

Number of bars:

$$A_b = \pi \frac{(14)^2}{4} = 153.94 \text{ mm}^2$$

$$n = \frac{595.2}{153.94} = 3.87 \approx 4$$

Use 4 ϕ 14mm / m'

Spacing:

$$S = \frac{1000}{3.87} = 258 \text{ mm} \quad \text{Use } S=250 \text{ mm}$$

Check Spacing:

$$S_{\max} \leq 3 h$$

$$S_{\max} = 3 \times 150 = 450 \text{ mm}$$

$$S = 250 < S_{\max} = 450 \text{ mm} \quad \text{OK}$$

$$\text{Use } S = 250 \text{ mm}$$

$$\text{Use } \phi 14 \text{ mm @ } 250 \text{ mm}$$

IV.2. Negative Moment Reinforcement:

The connection zone (slab-landing) should be reinforced as a equal: a *half quantity of Positive moment*

$$A_s = \frac{595.2}{2} = 297.6 \text{ mm}^2$$

$$\text{Use } \phi = 12 \text{ mm} \quad A_b = \frac{\pi(12)^2}{4} = 113 \text{ mm}^2$$

$$n = \frac{297.6}{113} = 2.63 \approx 3$$

$$\text{Use } 3\phi 12 \text{ mm / m}$$

Spacing

$$S = \frac{1000}{2.63} = 380 \text{ mm}$$

$$\text{Use } \phi 12 \text{ mm @ } 380 \text{ mm}$$

Check Spacing:

$$S_{\max} \leq 3 h$$

$$S_{\max} = 3 \times 150 = 450 \text{ mm}$$

$$S = 380 < S_{\max} = 450 \text{ mm} \quad \text{OK}$$

$$\text{Use } S = 380 \text{ mm}$$

$$\text{Use } \phi 12 \text{ mm @ } 380 \text{ mm}$$

IV.3. Temperature and Shrinkage Reinforcement:

$$\text{Use } \phi 10 \text{ mm}$$

Steel Ratio:

$$\rho_{\min} = \frac{0.0018 \times 400}{f_y}$$

$$\rho_{\min} = \frac{0.0018 \times 400}{400} = 0.0018$$

Effective Depth:

$$d = h - cc - \phi_b(\text{main}) - \frac{\phi_b(\text{temp})}{2}$$

$$d = 150 - 20 - 14 - \frac{10}{2} = 111 \text{ mm}$$

Steel Area:

$$A_s = \rho_{\min} \times b \times d$$

$$= 0.0018 \times 1000 \times 111 = 199.8 \text{ mm}^2$$

Number of bars

$$A_b = \pi \frac{(10)^2}{4} = 78.5 \text{ mm}^2$$

$$n = \frac{199.8}{78.5} = 2.54 \approx 3$$

Use 3 ϕ 10mm / m'

Spacing:

$$S = \frac{1000}{2.54} = 393 \text{ mm}$$

Use s=380 mm

Check spacing

$$S_{\max} \leq 3h = 3 \times 150 = 450 \text{ mm}$$

$$S = 380 \leq S_{\max} = 450 \text{ mm}$$

Use ϕ 10 mm @ 380 mm

IV.4. Shear:

$$\phi V_c = \phi \left[\frac{\sqrt{f_c'}}{6} \right] \times b_w \times d$$

$$= 0.85 \times \frac{\sqrt{25}}{6} \times 1000 \times 124 \times 10^{-3} = 87.83 \text{ kN}$$

$$V_u = R_A = 31 \text{ kN}$$

$$V_u < \phi V_c \Rightarrow \text{o.k}$$

No shear stirrups need

V. BEAM STEEL REINFORCEMENT

V.1. Dimension of Beam:

Deflection conditions.

$$h_{\min} = \frac{L}{16} \quad (\text{Simply supported beam})$$

$$h_{\min} = \frac{6000}{16} = 375 \text{ mm Use } h = 400 \text{ mm}$$

$$d = h - cc - \phi_{sb} - \frac{\phi_b}{2}$$

$$d = 400 - 20 - 10 - \frac{16}{2} = 362 \text{ mm}$$

$$\left(\frac{h}{3} < b < \frac{2h}{3} \right)$$

$$\left(\frac{400}{3} < b < \frac{2 \times 400}{3} \right) = (133.3 < b < 266.6)$$

Use $b = 200 \text{ mm}$

V.2. Loads on the Beam

$$\text{Reaction of R. stair slab:} \quad = 28.45 \text{ kN/m}$$

$$\text{Load from landing:} \quad 0.15 \times 1.1 \times 24 = 43.96 \text{ kN/m}$$

$$\text{Own weight} \quad 0.4 \times 0.2 \times 24 = 1.92 \text{ kN/m}$$

$$\text{Weight of wall:} \quad = 7.5 \text{ kN/m}$$

$$\text{Total dead load} \quad = 28.45 + 3.96 + 1.92 + 7.5 = 41.83 \text{ kN/m}$$

$$U = (1.2 \times DL) + (1.6 \times LL)$$

$$U_3 = (1.2 \times 41.83) + (1.6 \times 5) = 58.2 \text{ kN/m}$$

V.3 Structural Analysis for Beam

- Reaction:

$$R = \frac{Ul}{2} = \frac{58.2 \times 6}{2} = 174.6 \text{ kN}$$

- Moments:

$$M = \frac{Ul^2}{24} = \frac{58.2(6)^2}{24} = 87.3 \text{ kN.m} \quad (\text{Continuous beam})$$

- Diagrams:

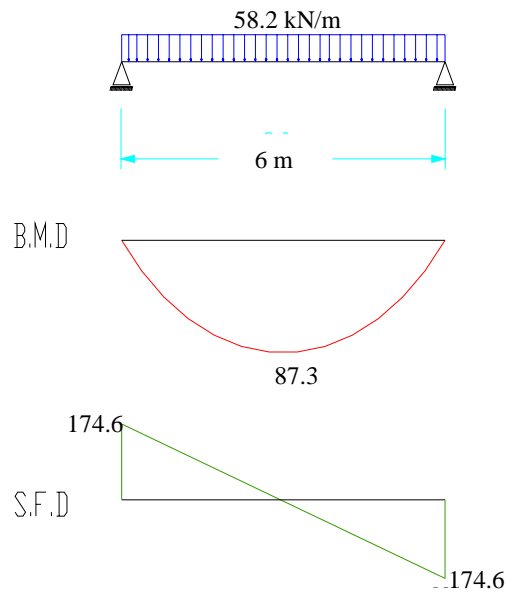


Figure: (7.6): Structural Analysis of Stair Beam

V.4. Structural Design for beam:

$$M_u = 87.3 \text{ kN.m}$$

$$M_n = \frac{M_u}{0.9} = \frac{87.3}{0.9} = 97 \text{ kN.m}$$

$$d = 362 \text{ mm} \quad b = 200 \text{ mm}$$

$$f'_c = 25 \text{ MPa} \quad f_y = 400 \text{ MPa}$$

Area of Steel:

$$m = \frac{f_y}{0.85 f'_c} = \frac{400}{0.85 \times 25} = 18.81$$

$$R_n = \frac{M_n}{bd^2} = \frac{97}{1000(0.2) \times (0.362)^2} = 3.7$$

$$\rho = \frac{1}{m} \left[1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right]$$

$$\rho = \frac{1}{18 \cdot 81} \left[1 - \sqrt{1 - \frac{2 \times 18 \cdot 81 \times 3.7}{400}} \right]$$

$$\rho = 0.010 \approx 0.010$$

Check ρ

$$\rho_{\min} = \frac{1.4}{f_y} = 0.0035$$

$$\rho_{\max} = 0.75 \left[0.85 \times 0.85 \times \frac{25}{400} \times \left(\frac{600}{600 + 400} \right) \right] = 0.02$$

$$\rho_{\min} = 0.0035 < \rho = 0.010 < \rho_{\max} = 0.02$$

$$A_s = \rho \cdot b \cdot d = 0.010 \times 200 \times 362 = 724 \text{ mm}^2$$

$$A_b = \pi \frac{(16)^2}{4} = 201 \text{ mm}^2$$

Number of steel:

$$n = \frac{724}{201} = 3.6 \approx 4$$

Use 4 ϕ 16mm/m'

Spacing:

$$S = \frac{b - 2cc - 2\phi_{sb} - n\phi_b}{n - 1}$$

$$S = \frac{200 - 2 \times 25 - 2 \times 10 - 4 \times 16}{3} = \frac{66}{3} = 22 \text{ mm}$$

$$S = 22 \text{ mm}$$

VI. STRUCTURAL DESIGN:

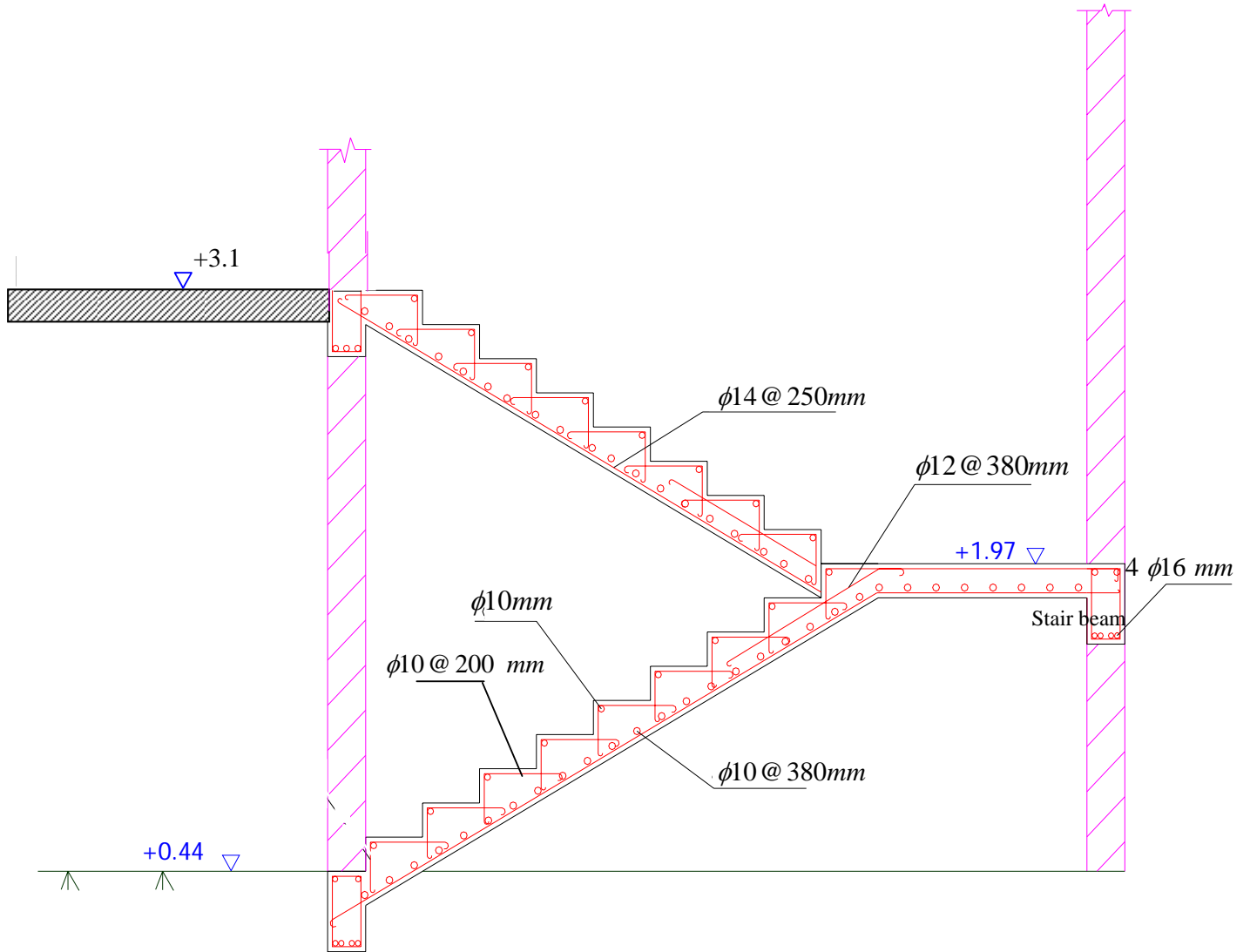


Figure (7.7): Reinforcement Detailing of Principal stair

7.5. EMERGENCY STAIR

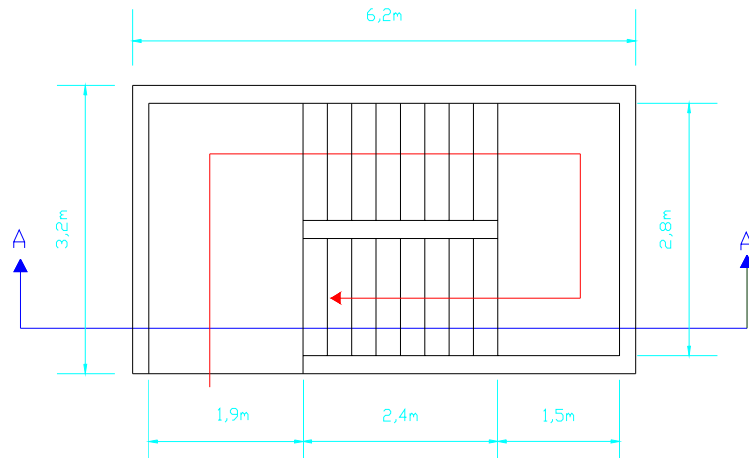


Figure (7.8): Horizontal of an Emergency Stair Dimensions

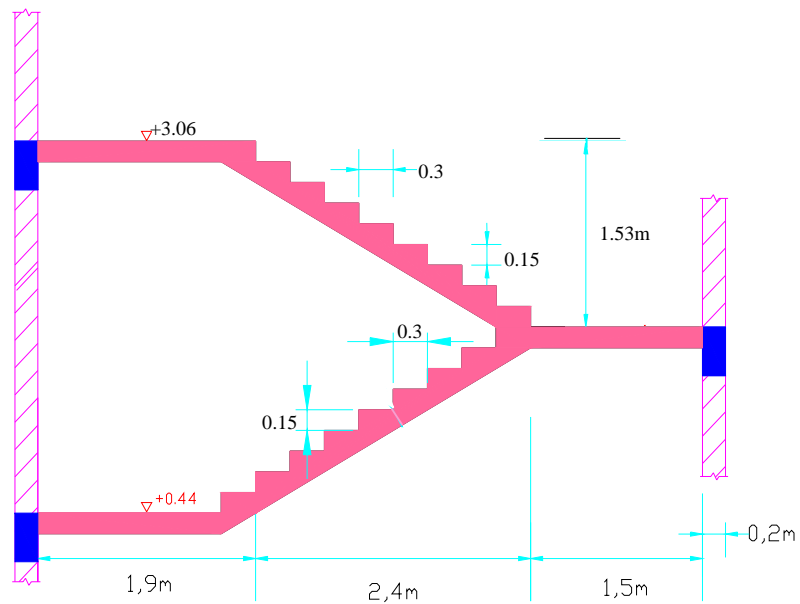


Figure (7.9): Heights of Emergency Stair

I. DIMENSIONS:**I.1. Slope Angle of the Stair Slab:**

$$\theta = \tan^{-1} \frac{1.53}{2.4} = 32.5^\circ$$

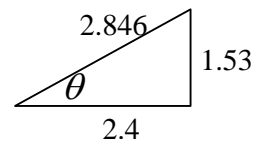
I.2. Length of Stair:

$$L = 2846 \text{ mm}$$

I.3. Thickness of Stair:

$$h = \frac{L}{21} = \frac{2846}{21} = 135.5 \text{ mm} \quad (\text{Both end continuous slabs})$$

Use $h = 150 \text{ mm}$

II. LOAD CALCULATIONS**II.1. Calculation of Load of Stair Slab**

Weight of stair slab:

$$= 0.15 \times 1 \times 1 \times 24 = 3.6 \text{ kN./m}^2$$

Weight of steps:

$$= \frac{1}{2} \times 0.3 \times 0.15 \times 24 = 0.54 \text{ kN/m}^2$$

Finishing:

$$= 1.24 \text{ kN/m}^2$$

Additional load:

$$= 0.62 \text{ kN/m}^2$$

Total load:

$$\sum DL = 6 \text{ kN/m}^2$$

$$\sum L.L = 5 \text{ kN/m}^2$$

$$U_1 = 1.2 \times 6 + 1.6 \times 5 = 15.2 \text{ kN/m}^2$$

II.2. Calculation of Load of Stair Landing

Weight of landing:

$$= 0.15 \times 1 \times 1 \times 24 = 3.6 \text{ kN/m}^2$$

Finishing:

$$= 1.25 \text{ kN/m}^2$$

Additional weight: $= 0.45 \text{ kN/m}^2$

$$\sum DL = 5.30 \text{ kN/m}^2$$

$$\sum L.L = 5 \text{ kN/m}^2$$

Design load:

$$U_2 = 1.2 \times 5.3 + 5 \times 1.6 = 14.36 \text{ kN/m}^2$$

III. STRUCTURAL ANALYSIS:

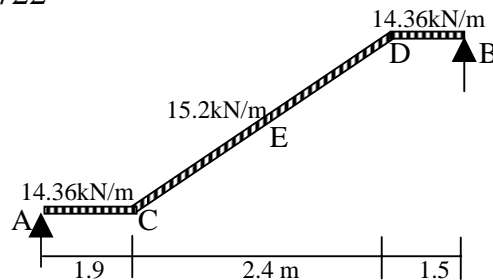
III.1. Reactions

$$\begin{aligned} \sum M_A = 0 &= (14.36 \times 1.9) \times 0.95 + (15.2 \times 2.4) \times 3.1 + (14.36 \times 1.5) \times 5.05 - 5.8 R_B \\ 0 &= 25.92 + 113.088 + 108.78 - 5.8 R_B \end{aligned}$$

$$R_B = \frac{247.788}{5.8} = 42.722 \text{ kN}$$

$$\begin{aligned} \sum Y = 0 &= (14.36 \times 1.9) + (15.2 \times 2.4) + (14.36 \times 1.5) \times 46.68 - 42.722 - R_A \\ R_A &= 27.284 + 36.48 + 21.54 - 42.722 \end{aligned}$$

$$R_A = 42.582 \text{ kN}$$



III.2. Moments

- The positive moment

$$\begin{aligned} M_C &= -(14.36 \times 1.9) \times 0.95 + 42.722 \times 1.9 \\ &= -25.92 + 80.91 = 54.99 \text{ kN.m} \end{aligned}$$

$$\begin{aligned} M_E &= (14.36 \times 1.9) \times (0.95 + 1.2) + (15.2 \times 1.2) \times 0.6 - 42.722 \times 3.1 \\ &= (14.36 \times 1.9) \times 2.15 + (15.2 \times 1.2) \times 0.6 - 42.722 \times 3.1 \\ &= 58.661 + 10.944 - 132.438 = -62.83 \text{ kN.m} \end{aligned}$$

$$M_u = 62.82 \text{ kN.m}$$

$$M_n = \frac{M_u}{0.9} = \frac{62.83}{0.9} = 69.815 \text{ kN.m}$$

III.3. Diagrams

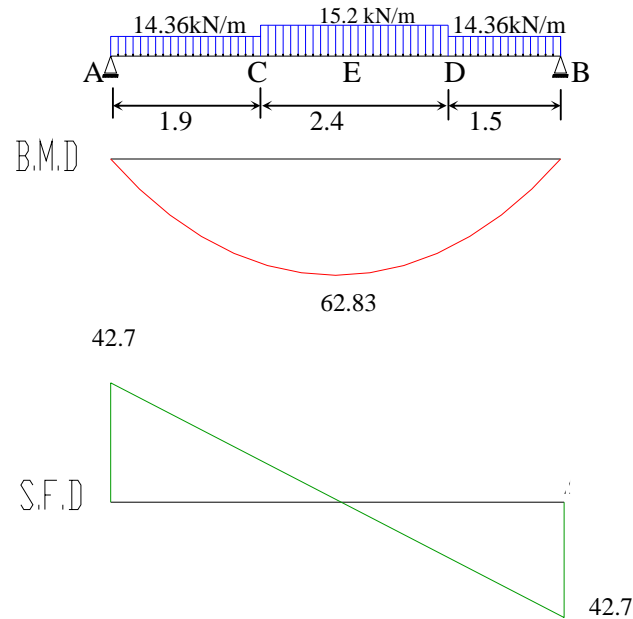


Figure (7.10): Structural Analysis of Emergency Stair Slab

IV. Calculation of Steel Reinforcement

IV.1. Design for Positive Moment:

Use ϕ 16mm, concrete over 20mm

$$f'_c = 25 \text{ MPa} \quad , \quad f_y = 400 \text{ MPa} \quad , \quad M_n = 69.83 \text{ kN.m}$$

Effective depth:

$$\begin{aligned} d &= h - \frac{\phi_b}{2} - cc \\ &= 150 - \frac{16}{2} - 20 = 122 \text{ mm} \end{aligned}$$

Area of steel:

$$m = \frac{f_y}{0.85 f'_c} = \frac{400}{0.85 \times 25} = 18.81$$

$$R_n = \frac{M_n}{bd^2} = \frac{69.83}{1000 \times (0.122)^2} = 4.69$$

$$\rho = \frac{1}{m} \left[1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right]$$

$$\rho = \frac{1}{18.81} \left[1 - \sqrt{1 - \frac{2 \times 18.81 \times 4.69}{400}} \right]$$

$$\rho = 0.0134$$

Check ρ

$$\rho_{\min} = \frac{1.4}{f_y} = 0.0035$$

$$\rho_{\max} = 0.75 \left[0.85 \times 0.85 \times \frac{25}{400} \times \left(\frac{600}{600 + 400} \right) \right] = 0.02$$

$$\rho_{\min} = 0.0035 < \rho = 0.0134 < \rho_{\max} = 0.02$$

$$A_s = \rho \cdot b \cdot d = 0.0134 \times 1000 \times 122 = 1634.8 \text{ mm}^2$$

Number of bars:

$$A_b = \pi \frac{(16)^2}{4} = 201 \text{ mm}^2$$

$$n = \frac{1635}{201} = 8.13 \approx 8$$

Use $8\phi 16 \text{ mm} / \text{m}'$

Spacing:

$$S = \frac{1000}{8.13} = 123 \text{ mm}$$

Use $S=125 \text{ mm}$

Check Spacing:

$$S_{\max} \leq 3h$$

$$S_{\max} = 3 \times 150 = 450 \text{ mm}$$

$$S = 125 \leq S_{\max} = 450 \text{ mm} \quad \text{OK}$$

Use $S = 125 \text{ mm}$

Use $\phi 16 \text{ mm} @ 125 \text{ mm}$

IV.2. Negative Moment Reinforcement:

Reinforcement connection zone (slab-landing) to be half quantity of Positive moment

$$A_s = \frac{1635}{2} = 817.5 \text{ mm}^2$$

$$A_b = \pi \frac{(16)^2}{4} = 201 \text{ mm}^2$$

$$n = \frac{817.5}{201} = 4.07 \approx 4$$

Use $4\phi 16\text{mm}/\text{m}'$

Spacing:

$$S = \frac{1000}{4.07} = 245 \text{ mm}$$

Use $S=250 \text{ m}$

Check Spacing:

$$S_{\max} \leq 3 h$$

$$S_{\max} = 3 \times 150 = 450 \text{ mm}$$

$$S = 250 \leq S_{\max} = 450 \text{ mm} \quad \text{OK}$$

Use $S = 250 \text{ mm}$

Use $\phi 16\text{mm} @ 250\text{mm}$

IV.3. Reinforcement Temperature and Shrinkage:

Use $\phi 10\text{mm}$

$$\rho = \frac{0.018 \times 400}{f_y} = 0.018$$

$$d = 150 - 20 - 16(\text{main}) - \frac{10}{2} = 109 \text{ mm}$$

$$A_s = 0.018 \times 1000 \times 109 = 196.2 \text{ mm}^2$$

$$n = \frac{196.2}{78.5} = 2.5 \approx 3$$

Use $3\phi 10\text{mm}/\text{m}'$

Spacing:

$$S = \frac{1000}{2.5} = 400 \text{ mm}$$

Use $S = 400 \text{ mm}$

$\phi 10 @ 400 \text{ mm}$

IV.4. Shear

$$\phi V_c = 0.85 \times \frac{\sqrt{25}}{6} \times 1000 \times 142 \times 10^{-3} = 100.6 \text{ kN}$$

$$V_u = 50 \text{ kN}$$

$$V_u < \phi V_c \text{ o.k}$$

V. BEAM STEEL REINFORCEMENT:**V.1. Dimensions**

$$h_{\min} = \frac{L}{16}$$

$$h_{\min} = \frac{3200}{16} = 200 \text{ mm}$$

Use $h = 400 \text{ mm}$

Effective depth and width :

$$d = h - cc - \phi_{sb} - \frac{\phi_b}{2}$$

$$= 400 - 20 - 10 - \frac{14}{2} = 363 \text{ mm}$$

$$\left(\frac{h}{3} < b < \frac{2h}{3} \right) \left(\frac{400}{3} < b < \frac{2 \times 400}{3} \right) = (133.3 \text{ mm} < b < 266.7 \text{ mm})$$

Use $b = 200 \text{ mm}$

V.2. Loads Acting on Beam

Reactions of R. slab and landing: $= 42.7 \text{ kN/m}$

Own Weight $0.2 \times 0.4 \times 24 = 1.92 \text{ kN/m}$

Weight of wall $= 7.5 \text{ kN/m}$

Total dead load: $= 52.12 \text{ kN/m}$

V.3 Structural Analysis for Beam

- Reaction:

$$R = \frac{U l}{2} = \frac{52.12 \times 3.2}{2} = 83.39 \text{ kN}$$

- Moments:

$$M = \frac{U l^2}{24} = \frac{52.12(3.2)^2}{24} = 66.72 \text{ kN.m}$$

- Diagrams:

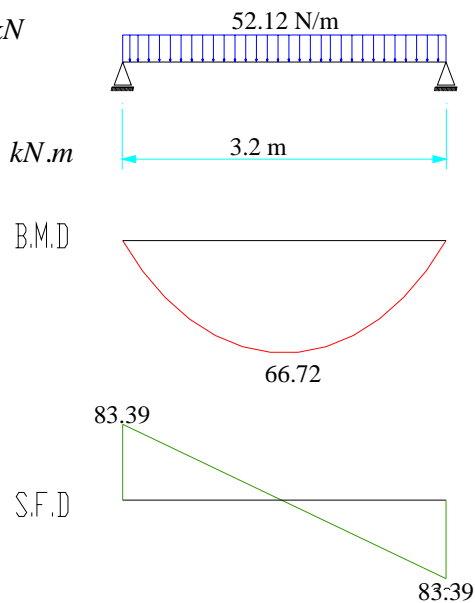


Figure (7.11): Structural Analysis of Emergency Stair Beam

V.4. Structural Design

$$d = 400 - 20 - 10 - 7 = 363 \text{ mm}$$

$$M_n = \frac{66.12}{0.9} = 73.47 \text{ kN.m/m}$$

Area of steel:

$$m = \frac{f_y}{0.85 f_c} = \frac{400}{0.85 \times 25} = 18.81$$

$$R_n = \frac{M_n}{b d^2} = \frac{88}{1000 \times 0.200 \times (0.363)^2} = 2.94$$

$$\rho = \frac{1}{m} \left[1 - \sqrt{1 - \frac{2mR_n}{f_y}} \right]$$

$$\rho = \frac{1}{18.81} \left[1 - \sqrt{1 - \frac{2 \times 18.81 \times 2.94}{400}} \right]$$

$$\rho = 0.009$$

Check ρ

$$\rho_{\min} = \frac{1.4}{f_y} = 0.0035$$

$$\rho_{\max} = 0.75 \left[0.85 \times 0.85 \times \frac{25}{400} \times \left(\frac{600}{600 + 400} \right) \right] = 0.02$$

$$\rho_{\min} = 0.0035 < \rho = 0.0079 < \rho_{\max} = 0.02$$

$$A_s = \rho \cdot b \cdot d = 0.0079 \times 200 \times 363 = 573.54 \text{ mm}^2$$

Number of bars:

$$A_b = \pi \frac{(14)^2}{4} = 153.9 \text{ mm}^2$$

$$n = \frac{573.54}{153.9} = 3.7 \approx 4$$

Use $4\phi 14 \text{ mm/m'}$

Spacing:

$$S = \frac{b - 2cc - 2\phi_{sb} - n\phi_b}{n - 1}$$

$$S = \frac{200 - 2 \times 25 - 2 \times 10 - 4 \times 14}{3} = 24.7 \text{ mm}$$

$$S = 25 \text{ mm}$$

VI. STRUCTURAL DESIGN:

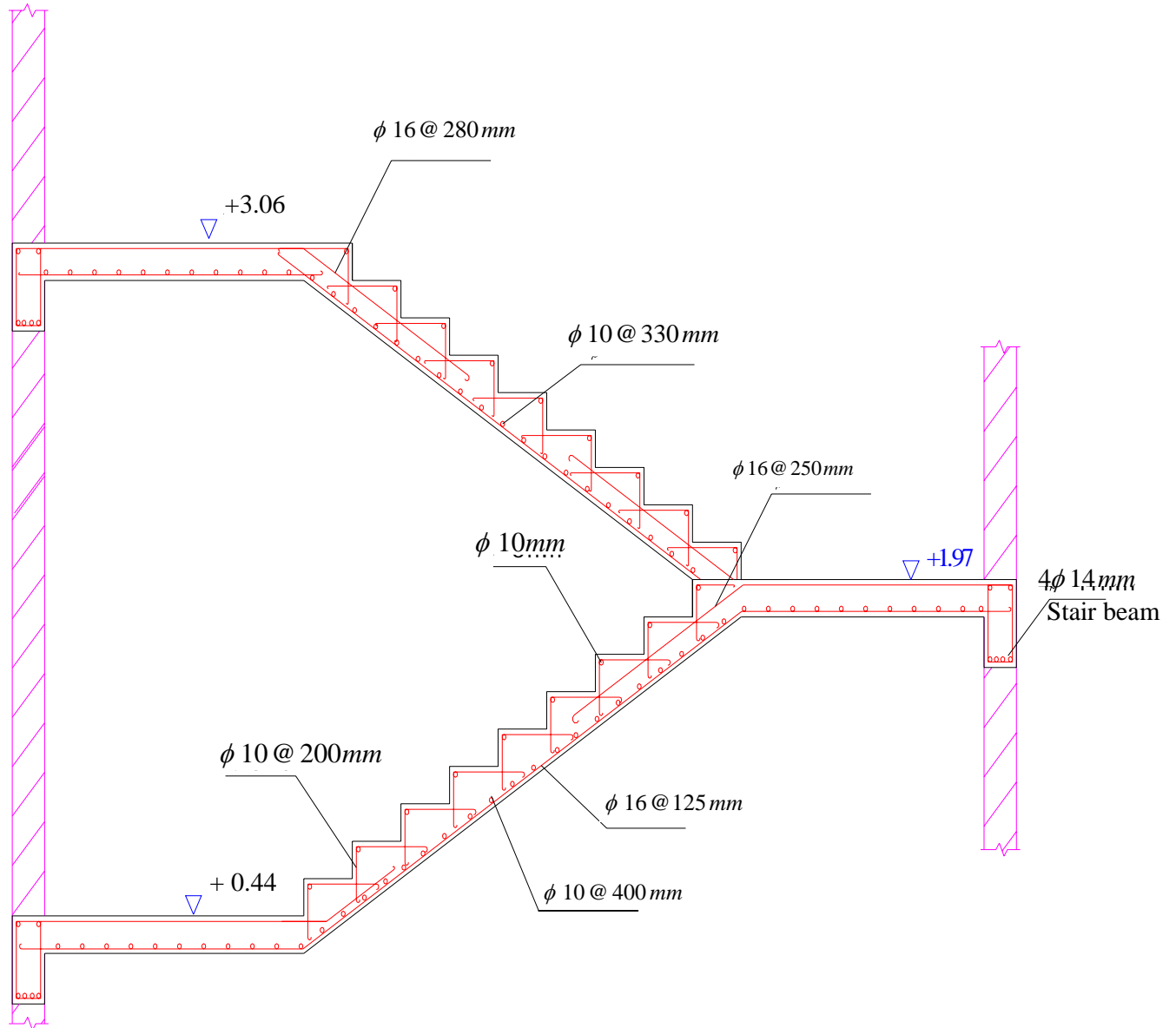


Figure (7.12): Details of Emergency Reinforcement Stairs